ACSC/STAT 3720, Life Contingencies I
Winter 2015
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Homework Sheet 8
Due: Wednesday 8th April: 10:30 PM

Basic Questions

1. A woman aged 36, who is a select life on Table 1 buys a 10-year term insurance policy with a death benefit of $600,000. (The policy uses a net annual premium.) Five years later, she wants to surrender the policy. The interest rate is $i = 0.02$. If the insurance company pays a cash surrender value of 80% of the policy value, how much does she receive?

2. A man aged 46 buys mortgage insurance on a mortgage for $200,000 at $i = 0.04$ with annual repayments of $13,839.77, for 22 years. The mortgage insurance pays off the outstanding balance on this mortgage at the time the individual dies. The individual is a select life on Table 1. The interest rate used to value the insurance contract is $i = 0.04$. The annual premiums for this mortgage insurance are therefore $193.58. Two years later, the man sells the house and wants to cancel the policy. Use the retrospective method to calculate the policy value at that time.

3. A man aged 53, who is a select life on Table 1 buys a 10-year endowment insurance with a benefit of $700,000. The interest rate is $i = 0.08$, which gives $A_{[53]} = 0.0729141$, $A_{[53]+1} = 0.0778819$, $A_{[53]+4} = 0.0937116$ and $A_{[53]+10} = 0.132398$. Using a Full preliminary term of 1 year, calculate the policy value after 4 years.

Standard Questions

4. A woman aged 43, who is a select life on Table 1 buys a 10-year term insurance policy with a death benefit of $500,000. The interest rate is $i = 0.05$, so $A_{[43]:\overline{10|}} = 0.614981$. Five years later, she wants to convert the policy to a whole life insurance. If the insurance company pays a cash surrender value of 85% of the policy value, and the woman goes through the underwriting process again, so that she is a select life at age 48, what is the new premium for the whole life insurance policy $[A_{[48]} = 0.133980.]$?

5. A man bought a whole life insurance policy 4 years ago. At the time, his age was 47, and he was rated a select life following Table 1. The benefit of the policy was $800,000. The interest rate is $i = 0.05$. He now wants to convert the policy to a paid-up term policy with the same death benefit. The insurance company offers a cash surrender value of 85% of the policy value. What is the term new of the new insurance contract? $[A_{[47]} = 0.128315, A_{51} = 0.153031]$

Bonus Question

6. A woman aged 29 bought a 10-year term insurance with annual premiums. At the time, she was a select life from Table 1. If she is in good health 5 years later, she would be able to

surrender her current policy and use the money to purchase a 5-year term insurance for the same death benefit. Since she is now a select life, she would benefit from a lower premium. What cash surrender value should the insurance company offer her, so that this option results in the same premiums as her current policy? The current interest rate is $i = 0.06$.

Table 1: Select lifetable to be used for questions on this assignment

x	$l_{[x]}$	$l_{[x]+1}$	$l_{[x]+2}$	$l_{[x]+3}$	x	$l_{[x]}$	$l_{[x]+1}$	$l_{[x]+2}$	$l_{[x]+3}$
25	9998.75	9997.65	9996.30	9994.66	74	8987.73	8932.10	8862.49	8775.52
26	9997.00	9995.83	9994.40	9992.66	75	8897.04	8836.71	8761.27	8667.10
27	9995.14	9993.90	9992.38	9990.52	76	8798.69	8733.34	8651.66	8549.78
28	9993.16	9991.84	9990.22	9988.24	77	8692.13	8621.41	8533.09	8423.00
29	9991.05	9989.65	9987.92	9985.80	78	8576.81	8500.36	8404.95	8286.16
30	9988.81	9987.30	9985.46	9983.18	79	8452.13	8369.60	8266.68	8138.66
31	9986.40	9984.80	9982.82	9980.38	80	8317.52	8228.53	8117.67	7979.93
32	9983.83	9982.11	9979.99	9977.37	81	8172.36	8076.57	7957.35	7809.41
33	9981.07	9979.23	9976.95	9974.13	82	8016.08	7913.13	7785.15	7626.56
34	9978.11	9976.13	9973.68	9970.64	83	7848.11	7737.67	7600.54	7430.89
35	9974.93	9972.79	9970.16	9966.88	84	7667.89	7549.66	7403.05	7221.99
36	9971.50	9969.20	9966.36	9962.82	85	7474.92	7348.64	7192.27	6999.51
37	9967.80	9965.33	9962.25	9958.44	86	7268.77	7134.21	6967.86	6763.22
38	9963.81	9961.14	9957.82	9953.69	87	7049.07	6906.07	6729.62	6513.04
39	9959.50	9956.61	9953.02	9948.55	88	6815.55	6664.05	6477.46	6249.02
40	9954.84	9951.71	9947.82	9942.98	89	6568.09	6408.10	6211.48	5971.42
41	9949.79	9946.41	9942.19	9936.94	90	6306.70	6138.35	5931.96	5680.73
42	9944.32	9940.66	9936.08	9930.38	91	6031.59	5855.15	5639.41	5377.67
43	9938.39	9934.41	9929.45	9923.26	92	5743.19	5559.08	5334.61	5063.27
44	9931.96	9927.64	9922.25	9915.52	93	5442.15	5250.97	5018.61	4738.86
45	9924.97	9920.28	9914.42	9907.10	94	5129.44	4931.97	4692.79	4406.12
46	9917.37	9912.28	9905.91	9897.94	95	4806.33	4603.54	4358.89	4067.08
47	9909.11	9903.58	9896.65	9887.98	96	4474.39	4267.51	4018.96	3724.10
48	9900.13	9894.11	9886.57	9877.13	97	4135.60	3926.04	3675.44	3379.91
49	9890.36	9883.80	9875.59	9865.30	98	3792.25	3581.66	3331.11	3037.57
50	9879.71	9872.57	9863.63	9852.42	99	3447.02	3237.23	2989.05	2700.39
51	9868.12	9860.34	9850.59	9838.38	100	3102.90	2895.94	2652.63	2371.88
52	9855.48	9847.01	9836.39	9823.08	101	2763.19	2561.21	2325.37	2055.64
53	9841.72	9832.48	9820.90	9806.39	102	2431.39	2236.61	2010.90	1755.27
54	9826.71	9816.64	9804.02	9788.18	103	2111.15	1925.80	1712.81	1474.18
55	9810.34	9799.37	9785.60	9768.33	104	1806.12	1632.34	1434.48	1215.44
56	9792.49	9780.52	9765.51	9746.67	105	1519.82	1359.55	1178.94	981.65
57	9773.03	9759.97	9743.60	9723.05	106	1255.46	1110.36	948.70	774.71
58	9751.79	9737.56	9719.69	9697.28	107	1015.81	887.14	745.58	595.71
59	9728.63	9713.10	9693.62	9669.17	108	802.96	691.49	570.56	444.87
60	9703.36	9686.43	9665.17	9638.51	109	618.23	524.17	423.71	321.41
61	9675.80	9657.33	9634.15	9605.07	110	462.04	385.00	304.13	223.65
62	9645.73	9625.59	9600.31	9568.61	111	333.80	272.80	210.00	149.10
63	9612.94	9590.98	9563.42	9528.85	112	231.99	185.53	138.71	94.62
64	9577.18	9553.24	9523.19	9485.52	113	154.19	120.34	87.07	56.74
65	9538.19	9512.09	9479.35	9438.30	114	97.30	73.90	51.50	31.84
66	9495.69	9467.25	9431.58	9386.86	115	57.78	42.55	28.41	16.52
67	9449.37	9418.39	9379.54	9330.85	116	31.92	22.69	14.43	7.81
68	9398.90	9365.17	9322.87	9269.88	117	16.15	11.04	6.63	3.30
69	9343.95	9307.23	9261.20	9203.55	118	7.34	4.79	2.69	1.21
70	9284.12	9244.18	9194.11	9131.43	119	2.90	1.79	0.93	0.37
71	9219.03	9175.59	9121.17	9053.07	120	0.95	0.55	0.26	0.09
72	9148.24	9101.03	9041.91	8967.97	121	0.23	0.13	0.05	0.01
73	9071.30	9020.03	8955.85	8875.63	122	0.03	0.02	0.01	0.00

3