# ACSC/STAT 4703, Actuarial Models II 

FALL 2023
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Homework Sheet 6
Due: Thursday 8th November: 14:30

## Basic Questions

1. An insurance company has the following previous data on aggregate claims:

| Policyholder | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Mean | Variance |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 76.04 | 5.33 | 872.93 | 0.00 | 0.00 | 190.860 | 146419.894 |
| 2 | 5.55 | 64.77 | 1421.35 | 542.52 | 2140.48 | 834.934 | 853717.609 |
| 3 | 33.12 | 10.10 | 108.50 | 0.00 | 173.90 | 65.124 | 5501.682 |
| 4 | 12.78 | 494.70 | 1578.16 | 87.65 | 32.21 | 441.100 | 442838.590 |
| 5 | 1728.19 | 0.00 | 2898.65 | 1570.46 | 24.30 | 1244.320 | 1528521.572 |

Calculate the Bühlmann credibility premium for each policyholder in Year 6 .
2. The file HW6_data.txt contains aggregate claim data from 100 policyholders over the past 10 years. Use this data to estimate the book premium and the credibility of 10 years' experience.
3. An insurance company collects the following numbers of claims from five policyholders over a 5 -year period.

| Policyholder | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 |
| :--- | ---: | ---: | ---: | ---: | ---: |
| 1 | 6 | 5 | 4 | 5 | 5 |
| 2 | 7 | 4 | 5 | 2 | 8 |
| 3 | 4 | 2 | 3 | 2 | 0 |
| 4 | 6 | 4 | 5 | 5 | 7 |
|  | 3 | 0 | 2 | 1 | 2 |

company assumes that the number of claims for each policyholder follows a Poisson distribution. Use Bühlmann credibility to estimate the average number of claims for Policyholder 4 in Year 6.

## Standard Questions

4. The file HW6_data2.txt contains aggregate claim data from 100 policyholders over the past 10 years. Some policyholders did not purchase insurance in all years. Use this data to estimate the book premium and the credibility of 10 years' experience.
5. Aggregate claims for a given individual policy are modelled as following a Gamma distribution with $\alpha=4 m_{i}$ and $\theta=R_{i}$, where $R_{i}$ is a risk factor for that policyholder that varies between individuals and $m_{i}$ is the exposure of the individual.
From a dataset of 100 policyholders with different exposures, they find that the total aggregate claim is $\$ 98,236$ from a total of 722 units of exposure. They also calculate:

$$
\begin{aligned}
\sum m_{i}^{2} & =11,604 \\
\sum m_{i} X_{i}^{2} & =16,850,495.1375
\end{aligned}
$$

where $X_{i}$ is the aggregate claims per unit of exposure for Policyholder $i$ (so $\sum m_{i} X_{i}=98236$ ). Estimate the EPV and VHM from this data.

