

ACSC/STAT 3720, Life Contingencies I  
Winter 2018  
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Homework Sheet 3  
Due: Wednesday 14th February: 12:30 PM

### Basic Questions

1. Calculate the expected benefit of a whole life insurance sold to an individual aged 105, if the death benefit is \$460,000 at the end of the year of death, the lifetable is Table 1, and the interest rate is  $i = 0.04$ .
2. Calculate the expected benefit, and the variance of the benefit of a 5-year endowment policy with benefit \$500,000 at the end of year of death of the policyholder or after 5 years, whichever comes first. The lifetable for this policy is Table 1, and the interest rate is  $i = 0.06$ . The policy is sold to a select individual aged 36.
3. A select individual aged 52 purchases a 5-year term insurance policy with a benefit of \$700,000 payable immediately upon the death of the individual. Force of interest is  $\delta = 0.038$ . The expected benefit from a 5-year term policy for this individual with payment at the end of year of death would be \$4,857.62. Using a uniform distribution of deaths assumption, calculate the expected benefit from the policy with payment immediately upon death.
4. An individual aged 36 wants to purchase whole life insurance that pays a benefit at the end of the year of death. The interest rate is  $i = 0.04$ . The individual has a number of dangerous hobbies and uses the special lifetable:

$x$	$l_x$	$d_x$
36	10000.00	15.81
37	9984.19	16.23
38	9967.96	16.71
39	9951.25	17.25
40	9934.00	17.86

After age 40, the individual will be too old to participate in these hobbies and will use a standard lifetable, which will give the value  $A_{40} = 0.143482$ . Calculate the EPV of the benefit for this individual from a whole-life policy which has a death benefit of \$400,000.

### Standard Questions

5. An individual aged 39 who follows the ultimate part of the lifetable in Table 1 has a 15-year endowment insurance with a benefit of \$600,000 payable at the end of the year of death or after 15 years, whichever is sooner. The individual wants to convert this to a whole life insurance policy. If the current interest rate is  $i = 0.04$ , what benefit for the whole life policy would have the same EPV as the endowment insurance policy? [The company has already calculated that  $A_{39} = 0.138327$  and  $A_{54} = 0.236372$ .]
6. A woman aged 35 buys a house with a mortgage of \$400,000. She amortises this amount with annual payments over a period of 25 years at  $i = 0.05$ . She takes out mortgage insurance,

which pays off the outstanding balance (principle plus interest) of the mortgage at the end of the year in which she dies. [Assume that the mortgage company does not charge a penalty for early repayment in this case.] If the insurance company uses an interest rate  $i = 0.03$  and the ultimate part of the life table from Table 1, calculate the expected present value of the benefit on this policy. You are given the following values, some of which may be useful:

$i$	$A_{35:\overline{26} }$
-0.03	2.1951
-0.02830189	2.09808
-0.02	1.68411
-0.01941748	1.65847
-0.01904762	1.64239
0.01904762	0.615276
0.01941748	0.609564
0.02	0.600679
0.02830189	0.487784
0.03	0.467563
0.05	0.285768
0.06	0.224397

Table 1: Select lifetable to be used for questions on this assignment

$x$	$l_{[x]}$	$l_{[x]+1}$	$l_{[x]+2}$	$l_{[x]+3}$	$x$	$l_{[x]}$	$l_{[x]+1}$	$l_{[x]+2}$	$l_{[x]+3}$
25	9998.75	9997.65	9996.30	9994.66	74	8987.73	8932.10	8862.49	8775.52
26	9997.00	9995.83	9994.40	9992.66	75	8897.04	8836.71	8761.27	8667.10
27	9995.14	9993.90	9992.38	9990.52	76	8798.69	8733.34	8651.66	8549.78
28	9993.16	9991.84	9990.22	9988.24	77	8692.13	8621.41	8533.09	8423.00
29	9991.05	9989.65	9987.92	9985.80	78	8576.81	8500.36	8404.95	8286.16
30	9988.81	9987.30	9985.46	9983.18	79	8452.13	8369.60	8266.68	8138.66
31	9986.40	9984.80	9982.82	9980.38	80	8317.52	8228.53	8117.67	7979.93
32	9983.83	9982.11	9979.99	9977.37	81	8172.36	8076.57	7957.35	7809.41
33	9981.07	9979.23	9976.95	9974.13	82	8016.08	7913.13	7785.15	7626.56
34	9978.11	9976.13	9973.68	9970.64	83	7848.11	7737.67	7600.54	7430.89
35	9974.93	9972.79	9970.16	9966.88	84	7667.89	7549.66	7403.05	7221.99
36	9971.50	9969.20	9966.36	9962.82	85	7474.92	7348.64	7192.27	6999.51
37	9967.80	9965.33	9962.25	9958.44	86	7268.77	7134.21	6967.86	6763.22
38	9963.81	9961.14	9957.82	9953.69	87	7049.07	6906.07	6729.62	6513.04
39	9959.50	9956.61	9953.02	9948.55	88	6815.55	6664.05	6477.46	6249.02
40	9954.84	9951.71	9947.82	9942.98	89	6568.09	6408.10	6211.48	5971.42
41	9949.79	9946.41	9942.19	9936.94	90	6306.70	6138.35	5931.96	5680.73
42	9944.32	9940.66	9936.08	9930.38	91	6031.59	5855.15	5639.41	5377.67
43	9938.39	9934.41	9929.45	9923.26	92	5743.19	5559.08	5334.61	5063.27
44	9931.96	9927.64	9922.25	9915.52	93	5442.15	5250.97	5018.61	4738.86
45	9924.97	9920.28	9914.42	9907.10	94	5129.44	4931.97	4692.79	4406.12
46	9917.37	9912.28	9905.91	9897.94	95	4806.33	4603.54	4358.89	4067.08
47	9909.11	9903.58	9896.65	9887.98	96	4474.39	4267.51	4018.96	3724.10
48	9900.13	9894.11	9886.57	9877.13	97	4135.60	3926.04	3675.44	3379.91
49	9890.36	9883.80	9875.59	9865.30	98	3792.25	3581.66	3331.11	3037.57
50	9879.71	9872.57	9863.63	9852.42	99	3447.02	3237.23	2989.05	2700.39
51	9868.12	9860.34	9850.59	9838.38	100	3102.90	2895.94	2652.63	2371.88
52	9855.48	9847.01	9836.39	9823.08	101	2763.19	2561.21	2325.37	2055.64
53	9841.72	9832.48	9820.90	9806.39	102	2431.39	2236.61	2010.90	1755.27
54	9826.71	9816.64	9804.02	9788.18	103	2111.15	1925.80	1712.81	1474.18
55	9810.34	9799.37	9785.60	9768.33	104	1806.12	1632.34	1434.48	1215.44
56	9792.49	9780.52	9765.51	9746.67	105	1519.82	1359.55	1178.94	981.65
57	9773.03	9759.97	9743.60	9723.05	106	1255.46	1110.36	948.70	774.71
58	9751.79	9737.56	9719.69	9697.28	107	1015.81	887.14	745.58	595.71
59	9728.63	9713.10	9693.62	9669.17	108	802.96	691.49	570.56	444.87
60	9703.36	9686.43	9665.17	9638.51	109	618.23	524.17	423.71	321.41
61	9675.80	9657.33	9634.15	9605.07	110	462.04	385.00	304.13	223.65
62	9645.73	9625.59	9600.31	9568.61	111	333.80	272.80	210.00	149.10
63	9612.94	9590.98	9563.42	9528.85	112	231.99	185.53	138.71	94.62
64	9577.18	9553.24	9523.19	9485.52	113	154.19	120.34	87.07	56.74
65	9538.19	9512.09	9479.35	9438.30	114	97.30	73.90	51.50	31.84
66	9495.69	9467.25	9431.58	9386.86	115	57.78	42.55	28.41	16.52
67	9449.37	9418.39	9379.54	9330.85	116	31.92	22.69	14.43	7.81
68	9398.90	9365.17	9322.87	9269.88	117	16.15	11.04	6.63	3.30
69	9343.95	9307.23	9261.20	9203.55	118	7.34	4.79	2.69	1.21
70	9284.12	9244.18	9194.11	9131.43	119	2.90	1.79	0.93	0.37
71	9219.03	9175.59	9121.17	9053.07	120	0.95	0.55	0.26	0.09
72	9148.24	9101.03	9041.91	8967.97	121	0.23	0.13	0.05	0.01
73	9071.30	9020.03	8955.85	8875.63	122	0.03	0.02	0.01	0.00