# ACSC/STAT 4703, Actuarial Models II 

Fall 2015
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Homework Sheet 7
Due: Friday 4th December: 10:30 PM

## Basic Questions

1. An insurance company sets the book pure premium for its car insurance premium at $\$ 836$. The expected process variance is 342,017 and the variance of hypothetical means is 86,202 . If an individual has no claims over the last 6 years, calculate the credibility premium for this individual's next year's insurance using the Bühlmann model.
2. An insurance company has the following data on a group life insurance policy:

| Year | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: |
| No. insured | 1,204 | 1,320 | 972 | 1,504 | 1,670 | 1,583 |
| No. of deaths | 8 | 3 | 7 | 9 | 11 | 10 |

The average mortality rate for the population is 1 death per 100 policies per year. The variance of hypothetical means of deaths per policy is 0.0014 . Using a Bühlmann-Straub model, calculate the credibility premium for this group insurance for Year 7.
3. An insurance company has the following previous data on aggregate claims:

| Policyholder | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 | Mean | Variance |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 0 | 445 | 0 | 0 | 877 | 1,198 | 420 | 268791.6 |
| 2 | 916 | 1,533 | 777 | 0 | 0 | 1,487 | 785.5 | 460396.3 |
| 3 | 709 | 0 | 0 | 1,275 | 924 | 0 | 484.6667 | 314534.3 |
| 4 | 1,910 | 2,004 | 3,723 | 714 | 1,410 | 422 | 1697.167 | 1383715 |
| 5 | 0 | 927 | 0 | 0 | 0 | 0 | 153.5 | 143221.5 |

Calculate the Bühlmann credibility premium for each policyholder in Year 7.
4. Over a three-year period, an insurance company observes the following numbers of claims:

| No. of claims | Frequency |
| ---: | ---: |
| 0 | 3,935 |
| 1 | 4,108 |
| 2 | 1,420 |
| 3 | 637 |
| 4 | 211 |
| 5 | 94 |
| 6 | 40 |
| 7 | 15 |
| 8 | 4 |
| 9 | 0 |
| 10 | 1 |

Some customers only had a two-year claim history. Claim frequencies for these customers were:

| No. of claims | Frequency |
| ---: | ---: |
| 0 | 670 |
| 1 | 482 |
| 2 | 289 |
| 3 | 104 |
| 4 | 38 |
| 5 | 9 |
| 6 | 2 |
| 7 | 1 |

Assuming the number of claims made by an individual in a year follows a Poisson distribution, calculate the credibility estimate for the expected claim frequency in the following year, of an individual who has made a total of 4 claims in the past 2 years.

## Standard Questions

5. Aggregate claims for a given insurance policy are modelled as following a log-normal, and experience indicates that $\sigma=1$ is the correct value. The first 4 years of experience on this policy are:

| Policyholder | Year 1 | Year 2 | Year 3 | Year 4 |
| :--- | ---: | ---: | ---: | ---: |
| 1 | 970 | 221 | 703 | 366 |
| 2 | 282 | 392 | 2934 | 1372 |
| 3 | 213 | 631 | 339 | 551 |
| 4 | 54 | 2383 | 252 | 647 |

(a) Estimate the EPV and VHM based on the MLE estimates for each $\mu$. [For a log-normal the MLE is $\hat{\mu}=\frac{\sum_{i=1}^{n} \log \left(X_{i}\right)}{n}$.]
(b) Calculate the credibility premium for policyholder 3 in the next year.
6. Claim frequency in a year for an individual follows a Poisson with parameter $\Lambda t$ where $\Lambda$ is the individual's risk factor and $t$ is the individual's exposure in that year. An insurance company collects the following data:

|  | Year 1 |  | Year 2 |  | Year 3 |  | Year 4 |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Policyholder | Exp | claims | Exp | claims | Exp | claims | Exp | claims |
| 1 | 45 | 12 | 10 | 6 | 45 | 14 | 14 | 2 |
| 2 | 27 | 0 | 12 | 0 | 74 | 0 | 27 | 0 |
| 3 | 10 | 9 | 293 | 149 | 14 | 6 | 13 | 5 |
| 4 | 10 | 0 | 14 | 3 | 17 | 2 | 6 | 2 |

In year 5, policyholder 3 has 64 units of exposure. Calculate the credibility estimate for claim frequency for policyholder 3 .

