# ACSC/STAT 4703, Actuarial Models II

## Winter 2020 Toby Kenney

**Instructor:** Toby Kenney

**Topics:** 

Department of Mathematics and Statistics

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Course Website: www.mathstat.dal.ca/~tkenney/4703/2020/

Office Hours: Monday 12:30–13:30, Tuesday 9:00-10:00, Thursday 11:30-12:30

Lectures: MWF: 13:35-14:25 LSC-COMMON C216

Aggregate Loss Models, Nonparametric Estimation, Bayesian Estimation, Model Selection, Credibility Theory, Pricing and

Reserving

**Textbook:** "Loss Models: From Data to Decisions" (Fourth Edition)

by S. A. Klugman, H. J. Panjer and G. E. Wilmot

published by Wiley, 2012

Additional References: Short-Term Actuarial Mathematics Study Note

by the Society of Actuaries (2017). Available at

https://www.soa.org/Files/Edu/2018/2018-ltam-loss-models-data.pdf

"Introduction to Ratemaking and Loss Reserving for Property and Casualty Insurance" (Fourth Edition), by R. L. Brown

and W. S. Lennox published by Actex, 2015

or (Third Edition), 2007, by R. L. Brown and L. R. Gottlieb

#### Course Work and method of assessment

There will be a midterm exam and a final exam. The midterm will be held in class on Friday 28th February, and should cover the material in Chapters 9 and 16, along with Chapters 2 and 4 of the additional reference *Introduction to Ratemaking and Loss Reserving for Property and Casualty Insurance*. The content of this exam may be changed, depending on the progress in lectures. The final exam will be arranged during the examination period 8–24th April.

There will also be about 8 homework assignments, which must usually be handed on Fridays in the lecture. After this, I will put the model solutions on the course website. No credit can be given for late homework. The overall homework mark will be made up of an average of the homework marks, with the exception of the worst mark for each student.

The homework sheet will be divided into 2 sections: The basic questions section tests the basic concepts covered in the course: everyone should be able to do all these questions. The standard questions section has questions where the concepts covered in the course can be applied to more realistic situations, or questions which involve a stronger theoretical insight; these questions are mostly straightforward, though there may be the occasional tricky question included. There may also be some bonus questions which are either more challenging, or else raise interesting or important issues that are not central to this course.

Occasionally a question may be started on one sheet, but continued on the following sheet, after the relevant material has been covered. In this case, the full question will be given on the earlier sheet, but the parts that should only be attempted with the later sheet are clearly marked, and are repeated on the later sheet. For some questions, I may occasionally give out a hint, rather than a complete model solution. Revised answers to these questions may then be submitted with the following week's homework.

Grades will be determined by performance in the exams and the weekly homeworks. The midterm exam counts for 30%, the final counts for 55%, while the homework counts for the remaining 15%. You must pass the final exam to obtain a passing grade in the course.

### Weekly Readings

Since class time is limited, I will be using it for explaining concepts and going over examples, rather than reading through the textbook. You should therefore read through the relevant sections of the textbook before the lecture, in order to gain the full benefit from the lecture. The sections of the textbook that will be covered each lecture will be listed on the website. This list may be updated from time to time, depending on the progress made in earlier lectures. Here is the current plan.

| Week  | Monday  | Wednesday   | Friday  |
|---|---|---|---|
| 6th January                                     | Introduction and Preliminaries,9 Aggregate Loss Models: 9.1 Introduction  | 9.2 Model choices, 9.3 The compound model for aggregate claims  | 9.4 Analytic results, 9.5 Computing the aggregate claims distribution   |
| 13th January                                    | 9.6 the recursive method  | 9.6.1 Applications to compound frequency models, 9.6.2 Overflow/Underflow problems  | 9.6.3 Numerical stability, 9.6.4 Continuous severity, 9.6.5 Constructing arithmetic distributions   |
| 20th January                                    | 9.7 The impact of individual policy modifications on aggregate payments   | 9.8 The individual risk model   | 9.8 The individual risk model (cont.)   |
| 27th January                                    | 16 Model selection: 16.3<br>Graphical comparison of density and distribution functions  | 16.4 Hypothesis tests   | 16.4 Hypothesis tests (cont.),Score-based approaches (AIC, BIC),16.5 Model Selection  |
| 3rd February                                    | IRLRPCI 2 Types of short-term insurance coverage:   | ing: 4.1 Introduction, 4.2<br>How outstanding claim payments arise, 4.3 Definition of terms   | MONROE DAY  |
| 10th February                                   | 4.4 Professional Considerations, 4.5 Checking the data, 4.6 Loss reserving methods  | 4.6 Loss reserving methods (cont.), 4.7 Discounting loss reserves   | Revision chapters 9, 16, IRL-RPCI 2, 4  |
|   |   |   |   |
| 17th February                                   |   | STUDY WEEK  |   |
| 17th February 24th February                     | Revision chapters 9, 16, IRL-RPCI 2, 4  | STUDY WEEK  Revision chapters 9, 16, IRL- RPCI 2, 4   | MIDTERM EXAM  |
|   |   | Revision chapters 9, 16, IRL-   | MIDTERM EXAM  18 Greatest accuracy credibility: 18.2 Conditional distributions and expectation, 18.3 Bayesian methodology   |
| 24th February                                   | RPCI 2, 4  17 Introduction and limited fluctuation credibility: 17.2 Limited fluctuation credibility theory, 17.3 Full  | Revision chapters 9, 16, IRL-RPCI 2, 4  17.4 Partial credibility, 17.5  | 18 Greatest accuracy credibility: 18.2 Conditional distributions and expectation,   |
| 24th February 2nd March                         | RPCI 2, 4  17 Introduction and limited fluctuation credibility: 17.2 Limited fluctuation credibility theory, 17.3 Full credibility  18.4 The credibility premium,   | Revision chapters 9, 16, IRL-RPCI 2, 4  17.4 Partial credibility, 17.5 Problems with this approach  18.5 The Buhlmann model (cont.), 18.6 The Buhlmann-Straub model, 18.7 exact   | 18 Greatest accuracy credibility: 18.2 Conditional distributions and expectation, 18.3 Bayesian methodology  18.7 exact credibility(cont.), 19 Empirical Bayes parameter estimation: 19.2   |
| 24th February 2nd March 9th March               | RPCI 2, 4  17 Introduction and limited fluctuation credibility: 17.2 Limited fluctuation credibility: 17.3 Full credibility  18.4 The credibility premium, 18.5 The Buhlmann model  19.2 Nonparametric estimation(cont.), 19.3 Semipara-  | Revision chapters 9, 16, IRL-RPCI 2, 4  17.4 Partial credibility, 17.5 Problems with this approach  18.5 The Buhlmann model (cont.), 18.6 The Buhlmann-Straub model, 18.7 exact credibility  IRLRPCI 3 Ratemaking: 3.1 Introduction, 3.2 Objectives of Ratemaking, 3.3 Fre-                   | 18 Greatest accuracy credibility: 18.2 Conditional distributions and expectation, 18.3 Bayesian methodology  18.7 exact credibility(cont.), 19 Empirical Bayes parameter estimation: 19.2 Nonparametric estimation  3.4 Data for ratemaking, 3.5  |
| 24th February  2nd March  9th March  16th March | RPCI 2, 4  17 Introduction and limited fluctuation credibility: 17.2 Limited fluctuation credibility: 17.3 Full credibility  18.4 The credibility premium, 18.5 The Buhlmann model  19.2 Nonparametric estimation(cont.), 19.3 Semiparametric estimation  3.6 The exposure unit, 3.7 The expected effective period, | Revision chapters 9, 16, IRL-RPCI 2, 4  17.4 Partial credibility, 17.5 Problems with this approach  18.5 The Buhlmann model (cont.), 18.6 The Buhlmann-Straub model, 18.7 exact credibility  IRLRPCI 3 Ratemaking: 3.1 Introduction, 3.2 Objectives of Ratemaking, 3.3 Frequency and Severity | 18 Greatest accuracy credibility: 18.2 Conditional distributions and expectation, 18.3 Bayesian methodology  18.7 exact credibility(cont.), 19 Empirical Bayes parameter estimation: 19.2 Nonparametric estimation  3.4 Data for ratemaking, 3.5 Premium data  IRLRPCI 5 Intermediate topics 5.1 Individual risk rating plans, 5.2 Increased limits |

#### Sections of the text covered

We expect to cover most of the material in Chapters 9 and 16–20 of Loss Models and also the material in Chapters 1–5 of Introduction to Ratemaking.

#### Students with disabilities

Students with disabilities are encouraged to register as quickly as possible at the Student Accessibility Services if they want to receive academic accommodations. To do so, plese 'phone 494-2836, email access@dal.ca, drop in at the Killam, G28, or visit our website at www.studentaccessibility.dal.ca.

### Plagiarism

Plagiarism is a serious academic offense which may lead to loss of credit, suspension or expulsion from the university. Please read the Policy on Intellectual Honesty contained in the Calendar or on the Dalhousie web site at: http://www.registrar.dal.ca/calendar/ug/UREG.htm#12.

### **Dalhousie Writing Centre**

Writing expectations at university are higher than you will have experienced at high school (or if you are entering a master's or PhD program, the expectations are higher than at lower levels). The Writing Centre is a Student Service academic unit that supports your writing development. Make an appointment to discuss your writing. Learning more about the writing process and discipline-specific practices and conventions will allow you to adapt more easily to your field of study.