## ACSC/STAT 4703, Actuarial Models II Fall 2020

Toby Kenney Homework Sheet 4 Due: Friday 13th March: 13:30 PM

## **Basic Questions**

1. An insurance company sells insurance. It estimates that the standard deviation of the aggregate annual claim is \$4,521 and the mean is \$1,020.

(a) How many years history are needed for an individual or group to be assigned full credibility? (Use r = 0.05, p = 0.90.)

The standard premium for this policy is \$1,020. A company has claimed a total of \$8,072 in the last 23 years.

(b) What is the Credibility premium for this company, using limited fluctuation credibility?

2. A home insurance company classifies houses as high, medium or low risk. Annual claims from high risk houses follow a Gamma distribution with  $\alpha = 4$  and  $\theta = 5000$ . Annual claims from medium risk houses follow a Gamma distribution with  $\alpha = 8$  and  $\theta = 1400$ . Annual claims from low risk houses follow a Gamma with  $\alpha = 14$  and  $\theta = 600$ . 15% of houses are high risk, 65% are medium risk and 20% are low risk.

(a) Calculate the expectation and variance of the aggregate annual claims from a randomly chosen home.

(b) Given that a homeowner's annual claims over the past 4 years are \$4,000, \$250 and \$1,100, what are the expectation and variance of the homeowner's claims next year?

## Standard Questions

3. For a certain insurance policy, the book premium is based on average claim frequency of 4.9 claims per year, and average claim severity of \$4,200. The standard for full credibility is 50 policy years for claim frequency and 230 claims for severity. The insurance company wants to change the standard for full credibility to a single standard (in terms of policy years) for aggregate claims. A particular group has 100 claims for a total of \$282,000, in 27 policy years of history. The insurance company wants the new standard to give the same premium for this group. What should the new standard be?

- 4. Aggregate claims for an individual are believed to follow a gamma distribution with  $\alpha = 0.8$  and  $\Theta$  varying between individuals. For a randomly chosen individual,  $\Theta$  follows an inverse gamma distribution with  $\alpha = 3$  and  $\theta = 2000$ . The insurance company uses limited fluctuation credibility with r = 0.05 and p = 0.95 to determine an individual's premium. If an individual has 6 years of past history, for what value of total claims during these 6 years would the limited fluctuation credibility premium equal the fair premium (using the Bayesian method)?
- 5. An insurance company has 4 years of past history on a marine insurance policy, denoted  $X_1$ ,  $X_2$ ,  $X_3$ ,  $X_4$ . It uses a formula  $\hat{X}_5 = \alpha_0 + \alpha_1 X_1 + \alpha_2 X_2 + \alpha_3 X_3 + \alpha_4 X_4$  to calculate the credibility premium in the fifth year. It has the following information on the policy:
  - In Year 1, the expected aggregate claim was \$32,000.
  - Expected aggregate claims increase by 4% per year.
  - The coefficient of variation of the aggregate claims is 0.8 in every year.
  - The correlation (recall  $\operatorname{Corr}(X, Y) = \frac{\operatorname{Cov}(X, Y)}{\sqrt{\operatorname{Var}(X)\operatorname{Var}(Y)}}$ ) between aggregate claims in years i and j is  $e^{-\frac{|i-j|}{2}}$  for all  $i \neq j$ .

Find a set of equations which can determine the values of  $\alpha_0$ ,  $\alpha_1$ ,  $\alpha_2$ ,  $\alpha_3$  and  $\alpha_4$ . [You do not need to solve these equations.]